

## CSC236 tutorial exercises, Week #7

### best before Thursday evening

These exercises are intended to give you practice proving facts about a recurrence.

1. Examine the recurrence  $R(n)$  below.

$$R(n) = \begin{cases} 0 & \text{if } n = 1 \\ n + 3R(\lceil n/3 \rceil) & \text{if } n > 1 \end{cases}$$

Last week we conjectured that if  $n = 3^k$  for some natural number  $k$ , then  $R(n) = n \log_3 n$ .

- (a) Use induction to prove this conjecture.
- (b) Emulate the lemma 3.6 on page 84 of the CSC236 notes, to prove that  $R$  is nondecreasing on natural numbers greater than, or equal to, 1.