

CSC236 fall 2018

correct after & before

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Using Introduction to the Theory of Computation,
Chapter 2

Outline

iterative binary search

power

notes



correctness by design

draw pictures of before, during, after

pre: A sorted, comparable with x

post: $0 \leq b \leq n$ and $A[0:b] < x \leq A[b:n-1]$



“derive” conditions from pictures

need notation for mutation



partial correctness

precondition+execution+termination imply postcondition

loop invariant helps get us closer



do we have termination?

correctness by discovery

integer power

```
def power(x, y) :  
    z = 1  
    m = 0  
    while m < y :  
        z = z * x  
        m = m + 1  
    return z
```

- ▶ precondition?
- ▶ postcondition?
- ▶ notation for mutation



partial correctness

precondition+execution+termination imply postcondition

a loop invariant helps get us closer



partial correctness

precondition+execution+termination imply postcondition

a loop invariant helps get us closer



prove partial correctness

prove termination

associate a decreasing sequence in \mathbb{N} with loop iterations

it helps to add claims to the loop invariant



put it together — correctness

notes