UNIVERSITY OF TORONTO Faculty of Arts and Science

term test #2, Version 1 CSC148H1S

Date: Wednesday March 14, 10:10–11:00 a.m. or 11:10–noon

Duration: 50 minutes

Instructor(s):

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No Aids Allowed

Name:	
utorid:	
U of T email:	

Please read the following guidelines carefully!

- Please write your name, utorid, and student number on the front of this exam.
- This examination has 4 questions. There are a total of 7 pages, DOUBLE-SIDED.
- Answer questions clearly and completely.
- You will receive 20% of the marks for any question you leave blank or indicate "I cannot answer this question."

Take a deep breath.

This is your chance to show us
How much you've learned.

We WANT to give you the credit Good luck!

1. [4 marks] tracing recursion Read the definition of function m1 below, then trace the calls on that function, using the tracing technique from class. Remember, if there are recursive sub-calls on lists you have evaluated above do not expand them further, just replace them by their values.

```
def m1(list_: list, num: int) -> int:
    """ docstring omitted! """
    if num == 1:
        return sum([1 for x in list_ if not isinstance(x, list)])
    elif num > 1:
        return sum([m1(x, num - 1) for x in list_ if isinstance(x, list)])
    else:
        return 0
```

(a) >>> m1([6], 1)

```
Solution
--> sum([1]) --> 1
```

(b) >>> m1([1, [2, 3, 4], 5], 1)

```
<u>Solution</u>
--> sum([1, 1]) --> 2
```

(c) >>> m1([7, [1, [2, 3, 4], 5], [6]], 2)

```
<u>Solution</u>
--> sum([m1([1, [2, 3, 4], 5], 1), m1([6], 1)]) --> sum([2, 1]) --> 3
```

(d) >>> m1([[7, [1, [2, 3, 4], 5], [6]]], 3)

```
Solution
--> sum([m1([7, [1, [2, 3, 4], 5] [6]], 2)]) --> sum([3]) --> 3
```

2. [6 marks] binary tree structure. Read the (very abbreviated!) declaration of BTNode below. Assume that the Python statements below the class declaration have been executed, then answer the questions. Hint: you may find it helpful to make a sketch of the tree.

(a) What is the data of t3's root node?

```
Solution
10
```

(b) What is the arity (branching factor) of the tree rooted at t3?

```
Solution 2
```

(c) Which of the tree rooted at t3's nodes is/are the leaves?

```
Solution
11, 12, 17
```

(d) Write down the values of the nodes if the tree rooted at t3 is visited in a postorder traversal.

```
Solution
11, 5, 7, 12, 17, 13, 10 (left)
```

17, 12, 13, 11, 5, 7, 10 (right)

(e) What is the length of the longest path in the tree rooted at t3?

Solution

3

(f) What is the height of the tree rooted at t3?

Solution

4

3. [5 marks] binary tree distance. Read the (very abbreviated) declaration of class BTNode below. Then implement the body of btnode_distance_sum. You may not assume any other functions or methods for binary tree nodes, unless you define them here.

```
from typing import Union
class BTNode:
    """Binary Tree node."""
    def __init__(self, data: object,
                 left: Union["BTNode", None]=None,
                 right: Union["BTNode", None]=None) -> None:
        Create BTNode (self) with data and children left and right.
        An empty BTNode is represented by None.
        self.data, self.left, self.right = data, left, right
def btnode_distance_sum(node: Union[BTNode, None], d: int) -> int:
    """ Return the sum of data at distance d from node.
    Assume all data in tree rooted at node is of type int
    and d is non-negative.
    >>> btnode_distance_sum(None, 1)
    >>> bt = BTNode(5, BTNode(6), BTNode(7))
    >>> btnode_distance_sum(bt, 7)
    >>> btnode_distance_sum(bt, 0)
    >>> btnode_distance_sum(bt, 1)
    13
    .....
```

Solution

```
node.data: int
if node is None:
    return 0
elif d < 0:
    return 0
elif d == 0:
    return node.data
else:
    return btnode_distance_sum(node.left, d - 1) + btnode_distance_sum(node.right, d - 1)</pre>
```

4. [5 marks] general tree. Read the (very abbreviated) declaration of class Tree below. Then implement the body of list_preorder. You may not use any functions or methods for trees unless you define them here.

```
class Tree:
    """
    Abbreviated Tree class
    """

    def __init__(self, value: object, children: List["Tree"]=None) -> None:
        """
        Create Tree self with content value and 0 or more children
        """
        self.value = value
        self.children = children[:] if children is not None else []

def list_preorder(t: Tree) -> list:
        """
        Return a list of t's values in preorder.

>>> list_preorder(Tree(0))
    [0]
    >>> t = Tree(1, [Tree(2, [Tree(3)]), Tree(4)])
    >>> list_preorder(t)
    [1, 2, 3, 4]
    """
```

```
Solution

if t.children == []:
    return [t.value]
else:
    return [t.value] + sum([list_preorder(c) for c in t.children], [])
```