

CSC148 winter 2018

reading recursion

week 6

Danny Heap

heap@cs.toronto.edu

BA4270 (behind elevators)

<http://www.teach.cs.toronto.edu/~csc148h/winter/>

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Outline

recursion on nested lists

recursion with turtles



summing lists

```
L1 = [1, 9, 8, 15]
```

```
sum(L1) = ???
```

```
L2 = [[1, 5], [9, 8], [1, 2, 3, 4]]
```

```
sum([sum(row) for row in L2]) = ??
```

```
L3 = [[1, 5], 9, [8, [1, 2], 3, 4]]
```

How can we sum L3?



hey! don't peek!

```
def sum_list(list_: List[int]) -> int:
    """
    Return the sum of all ints in list_.

    >>> sum_list([1, [2, 3], [4, 5, [6, 7], 8]])
    36
    >>> sum([])
    0
    """

    if isinstance(list_, list):
        return sum([sum_list(x) for x in list_])
    else:
        return list_
```



but wait: can you call a function before it's defined?

```
>>> def f(n):  
...     return g(n) + 1  
...  
>>> f(2) # CRASH!  
>>> def g(n):  
...     return 2 * n  
...  
>>> f(2)
```


depth of a list

Define the depth of `list_` as 1 plus the maximum depth of `list_`'s elements if `list_` is a list, otherwise 0.

- ▶ the definition is almost exactly the Python code you write!
- ▶ start by writing `return` and `pythonese` for the definition:

```
if isinstance(list_, list):
    return 1 + max([depth(x) for x in list_])
else: # list_ is not a list
    return 0
# find the bug! (then fix it...)
```

- ▶ deal with the special case of a non-list

trace to understand recursion

Trace in increasing complexity; at each step fill in values for recursive calls that have (basically) **already been traced**

- ▶ Trace `depth([])`
- ▶ Trace `depth(17)`
- ▶ Trace `depth([3, 17, 1])`
- ▶ Trace `depth([5, [3, 17, 1], [2, 4], 6])`
- ▶ Trace
`depth([14, 7, [5, [3, 17, 1], [2, 4], 6], 9])`



base case, general case

You will have noticed that a recursive function has a conditional structure that specifies how to combine recursive subcalls (general case), and when/how to stop (the base case, or cases).

What happens if you leave out the base case?

template for structural recursion

recursion when **input** is a recursive structure:

- ▶ if **input** cannot be decomposed into recursive sub-structures, you have a **base case** and you directly return a result without recursion
- ▶ if **input** can be decomposed into recursive sub-structures, solve them **recursively** and combine the result(s)

this reduces your job to (a) figuring out how to detect whether the input can be decomposed or not, (b) figuring out how what result to return for the base case, and (c) figuring out which substructures to solve recursively and how to combine their solutions



code for rec_max

```
if isinstance(list_, list):  
    return max([rec_max(x) for x in list_])  
else:  
    return list_
```



get some turtles to draw

Spawn some turtles, point them in different directions, get them to draw a little and then spawn again...

Try out `tree_burst.py`

Notice that `tree_burst` returns `NoneType`: we use it for its side-effect (drawing on a canvas) rather than returning some value.