

# CSC148 winter 2017

generative recursion, Exceptions,  
functional programming  
week 5

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## Outline

a1 topics

## idiomatic python

## getting that recursive insight for Tower of Hanoi

In order to implement a function that moves  $n$  cheeses from, say, stool 1 to stool 3, we'd first think of a name and parameters. We can start with `move_cheeses(n, source, dest)`, meaning show the moves from source stool to destination stool for  $n$  cheeses.



## stating that recursive insight:

The doodling on the previous slide breaks into a pattern, at least for the 2- and 3-cheese case:

- ▶ move all but the bottom cheese from source to intermediate stool (sounds recursive...)
- ▶ move the bottom cheese from the source to the destination stool (sounds like the 1-cheese move)
- ▶ move all but the bottom cheese from the intermediate to the destination stool (sounds recursive...)

The original problem repeats, except with different source, destination, and intermediate stools!

New name: `move_cheeses(n, source, intermediate, destination)`



## write some code!

fill in the three steps from the previous slide

```
def move_cheeses(n, source, intermediate, destination) -> None:
    """Print moves to get n cheeses from source to destination.

    @param int n:
    @param int source
    @param int intermediate:
    @param int destination:
    @rtype: None
    """
    if n > 1: # fill this in!
        move_cheeses(    ?,      ?,      ?,      ?)
        move_cheeses(    ?,      ?,      ?,      ?)
        move_cheeses(    ?,      ?,      ?,      ?)
    else: # just 1 cheese --- leave this out for now!
```



## complete that code!

Now, fill in what you do to move just one cheese — don't use any recursion! You will be returning a string that specifies you are moving from source to destination.

```
def move_cheeses(n, source, intermediate, destination) -> None:
    """Print moves to get n cheeses from source to destination.

    @param int n:
    @param int source
    @param int intermediate:
    @param int destination:
    @rtype: None
    """
    if n > 1: # fill this in!
        move_cheeses(    ?,      ?,      ?,      ?)
        move_cheeses(    ?,      ?,      ?,      ?)
        move_cheeses(    ?,      ?,      ?,      ?)
    else: # just 1 cheese --- leave this out for now!
        print(???)
```







## cause existing Exceptions:

- ▶ `int("seven")`

- ▶ `a = 1/0`

- ▶ `[1, 2][2]`



## raise existing Exceptions:

- ▶ `raise ValueError` or...
- ▶ `raise ValueError("you can't do that!")`



## roll your own Exceptions:

- ▶ `class ExtremeException(Exception):`  
    `pass`
- ▶ `raise ExtremeException`
- ▶ `raise ExtremeException('I really take exception`  
    `to that!')`





example: add (squares of) first 10 natural numbers

- ▶ You'll be generating a new list from `range(1, 11)`, so use a comprehension
- ▶ You want to add all the numbers in the resulting list, so use `sum`





# valid sudoku

what makes a sudoku square valid?

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

- ▶ valid rows
- ▶ valid columns
- ▶ valid subsquares



code it!

```
def valid_sudoku(grid, digit_set):  
    """  
    Return whether grid represents a valid, complete sudoku.  
  
    @type grid: list[list]  
    @type digit_set: set  
    @rtype: bool  
    """  
    assert all([len(r) == len(grid) for r in grid])  
    assert len(grid) == len(digit_set)  
    return (_all_rows_valid(grid, digit_set) and  
            _all_columns_valid(grid, digit_set) and  
            _all_subsquares_valid(grid, digit_set))
```





## code those non-existent helpers!

```
def _all_rows_valid(grid, digit_set):  
    """  
    Return whether all rows in grid are valid and complete.  
  
    @type grid: list[list]  
    @type digit_set: set  
    @rtype: bool  
  
    Assume grid has same number of rows as elements of digit_set  
    and grid has same number of columns as rows.  
    """  
    assert all([len(r) == len(grid) for r in grid])  
    assert len(grid) == len(digit_set)  
    return all([_list_valid(r, digit_set) for r in grid])
```



## code the helpers' helpers...

```
def _list_valid(r, digit_set):  
    """  
    Return whether r contains each element of digit_set  
    exactly once.  
  
    @type r: list  
    @type digit_set: set  
    @rtype: bool  
  
    Assume r has same number of elements as digit_set.  
    """  
    assert len(r) == len(digit_set)  
    return set(r) == digit_set
```

