

CSC148 winter 2017

reading recursion

week 4

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Outline

recursion on nested lists

recursion with turtles



distribute(handouts, raisedHands)

```
def distribute(handouts, raisedHands)
    if len(raisedHands) == 0 or len(handouts) == 1:
        keep handouts
    elif len(handouts) == 2:
        take 1 handout
        neighbour does distribute(1 handout, raisedHands)
    else:
        take 1 handout, split remainder into handouts/2
        2 neighbours do distribute(handouts/2, raisedHands)
```



summing lists

```
L1 = [1, 9, 8, 15]
```

```
sum(L1) = ???
```

```
L2 = [[1, 5], [9, 8], [1, 2, 3, 4]]
```

```
sum([sum(row) for row in L2]) = ??
```

```
L3 = [[1, 5], 9, [8, [1, 2], 3, 4]]
```

How can we sum L3?



re-use built-in... recursion!

- ▶ a function `sum_list` that adds all the numbers in a nested list shouldn't ignore built-in `sum`
- ▶ ...except `sum` wouldn't work properly on the nested lists, so make a list-comprehension of their `sum_lists`
- ▶ but wait, some of the list elements are numbers, not lists!

write a definition of `sum_list` — don't look at next slide yet!



hey! don't peek!

```
def sum_list(L):  
    """  
    Return the sum of all ints in L.  
  
    @param int|list[int|list[...]] L: possibly-nested list of ints, fin  
  
    >>> sum_list([1, [2, 3], [4, 5, [6, 7], 8]])  
    36  
    >>> sum([])  
    0  
    """  
  
    if isinstance(L, list):  
        return sum([sum_list(x) for x in L])  
    else:  
        return L
```



tracing recursion

To understand recursion, trace from simple to complex:

- ▶ `trace sum_list(17)`
- ▶ `trace sum_list([1, 2, 3])`. Remember how the built-in `sum` works...
- ▶ `trace sum_list([1, [2, 3], 4, [5, 6]])`. Immediately replace calls you've already traced (or traced something equivalent) by their value
- ▶ `trace sum_list([1, [2, [3, 4], 5], 6 [7, 8]])`. Immediately replace calls you've already traced by their value.

depth of a list

Define the depth of L as 1 plus the maximum depth of L 's elements if L is a list, otherwise 0.

- ▶ the definition is almost exactly the Python code you write!
- ▶ start by writing `return` and `pythonese` for the definition:

```
if isinstance(L, list):
    return 1 + max([depth(x) for x in L])
else: # L is not a list
    return 0
# find the bug! (then fix it...)
```

- ▶ deal with the special case of a non-list

trace to understand recursion

Trace in increasing complexity; at each step fill in values for recursive calls that have (basically) **already been traced**

- ▶ Trace `depth([])`
- ▶ Trace `depth(17)`
- ▶ Trace `depth([3, 17, 1])`
- ▶ Trace `depth([5, [3, 17, 1], [2, 4], 6])`
- ▶ Trace
`depth([14, 7, [5, [3, 17, 1], [2, 4], 6], 9])`

code for rec_max

```
if isinstance(L, list):  
    return max([rec_max(x) for x in L])  
else:  
    return L
```



nested_contains

Return whether a list, or any of its sublists, contain some non-list value.

- ▶ should return True if any element is equivalent to value
- ▶ should return True if any element is a list ultimately containing value
- ▶ Python `any` and functional `if` are useful

`<expression 1> if <condition> else <expression 2>`

If the condition is true, evaluates to the first expression, otherwise evaluates to the second expression.



template for structural recursion

recursion when **input** is a recursive structure:

- ▶ if **input** cannot be decomposed into recursive sub-structures, you have a **base case** and you directly return a result without recursion
- ▶ if **input** can be decomposed into recursive sub-structures, solve them **recursively** and combine the result(s)

this reduces your job to (a) figuring out how to detect whether the input can be decomposed or not, (b) figuring out how what result to return for the base case, and (c) figuring out which substructures to solve recursively and how to combine their solutions



get some turtles to draw

Spawn some turtles, point them in different directions, get them to draw a little and then spawn again...

Try out `tree_burst.py`

Notice that `tree_burst` returns `NoneType`: we use it for its side-effect (drawing on a canvas) rather than returning some value.