TI returned at end of lecture, on at leisure from BA4288

CSC148 winter 2016

reading recursion week 6

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http://www.cdf.toronto.edu/~csc148h/winter/ 416-978-5899

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#### Outline

test #1 follow-up

recursion on nested lists

recursion with turtles

#### announcements

- office hours, Monday/Wednesday/Thursday 3-5, BA4270 OR BA2230
- ▶ also CS help centre Wednesday and Thursday 4-6



# length, inter-section comparison

- ▶ mean of the 10 a.m. and 1 p.m. was a statistical tie, 6 p.m. was lower
- ▶ 6 p.m. mean is adjusted (0.5/30) higher
- overall average 67.9%
- be there was a lot of writing, see the proposal several slides on



### post-test exercise

- ▶ 1% post-test exercise, follow instructions on sticker, either on last page of test paper, or an inner page if there is no room
- exercise is due March 2nd, 11:59 p.m, not the date on the sticker!
- ▶ in testing there was an occasional error in submitting, which is fixed by reloading the web page and continuing



## fire alarm incident

- about 180 students had their test interrupted by a fire alarm
- our marking scheme has no provision for make-up tests; all likely dates overlap things such as assignment due dates or other course events
- ▶ for individuals who miss a test for valid reason, we re-evaluate the mark based on the second test and final
- consulting our department's undergraduate chair, we use a formula we believe neither gives an advantage nor a disadvantage to the affected students (see next slide)

### replace test #1 grade

 $a_1$ : class average on test #1  $a_2$ : class average on test #2

 $a_e$ : class average on on final exam

 $g_2$ : student's grade on test #2

 $g_e$ : student's grade on final exam

test #1 score: 
$$g_1 = \frac{g_2/a_2 + g_e/a_e}{2} \times a_1$$

rationale: student standing the same compared to the average on test #1 as compared to the average on test #2 and the final



#### what about those who didn't have a fire alarm?

although we think the formula for those who missed test #1 gives them neither an advantage nor a disadvantage, we will offer the remaining students the maximum of either their current grade on test #1 or the grade calculated using the formula on the previous slide

if a majority of students vote for this change, students who perform better relative to their peers on test #2 and the final may improve their test#1 grade

the vote will be in class, on March 2nd





## summing lists

How can we sum L3?



#### re-use built-in... recursion!

- ▶ a function sum\_list that adds all the numbers in a nested list shouldn't ignore built-in sum ← helpe
- ... except sum wouldn't work properly on the nested lists, so make a list-comprehension of their sum\_lists

but wait, some of the list elements are numbers, not lists!

# hey! don't peek!

```
def sum_list(L):
    ''' (list or int) -> int
    Return L if it's an int, or sum of the numbers in possibly nested 1
    >>> sum_list(17)
    17
    >>> sum_list([1, 2, 3])
    6
    >>> sum_list([1, [2, 3, [4]], 5])
    15
    , , ,
    # reuse: isinstance, sum, sum_list !
    if isinstance(L, list):
        return sum([sum_list(x) for x in L])
    else: # L is an int
        return L
```

## tracing recursion

To understand recursion, trace from simple to complex:

- ▶ trace sum\_list(17) → / 7
- trace sum\_list([1, 2, 3]). Remember how the built-in sum works... Sum([sum\_list(1), Sum\_list(3), Sum\_list(3))

  Sum([1, 2, 3])
- ▶ trace sum\_list([1, [2, 3], 4, [5, 6]]). Immediately replace calls you've already traced (or traced something equivalent) by their value
- m sheet
- ▶ trace sum\_list([1, [2, [3,4], 5], 6 [7, 8]]). Immediately replace calls you've already traced by their value.



# depth of a list

Define the depth of L as 1 plus the maximum depth of L's elements if L is a list, otherwise 0.

- ▶ the definition is almost exactly the Python code you write!
- start by writing return and pythonese for the definition:

```
if instance(L, list):
    return 1 + max([depth(x) for x in L])
else: # L is not a list
    return 0
# find the bug! (then fix it...)
```

Max is not befined on an empty his

deal with the special case of a non-list

> return non-list element



#### trace to understand recursion

Trace in increasing complexity; at each step fill in values for recursive calls that have (basically) already been traced



#### maximum number in nested list

#### Use the built-in max much like sum

- how would you find the max of non-nested list? max(...)
- how would you build that list using a comprehension? max([...])
- what should you do with list items that were themselves lists?

```
max([rec_max(x) ...])
```

▶ get some intuition by tracing through flat lists, lists nested one deep, then two deep...



## code for rec\_max

```
if isinstance(L, list):
    return max([rec_max(x) for x in L])
else:
    return L
```

#### trace the recursion

trace from simple to complex; fill in already-solved recursive calls

▶ trace rec\_max([4, 2, [3, 5, 1, 3, 4, 7], 8])

$$\longrightarrow \max\left( \left[ \text{ Yec-max}(4), \text{ Yec-max}(2) \right) \right)$$

$$\text{Yec-max}\left( \left[ 3, 5, 1, 3, 4, 7 \right] \right), \dots \right)$$

▶ trace

rec\_max([6, [4, 2, [3, 5, 1, 3, 4, 7], 8], 5])



### get some turtles to draw

Spawn some turtles, point them in different directions, get them to draw a little and then spawn again...

Try out tree\_burst.py

Notice that tree\_burst returns NoneType: we use it for its side-effect (drawing on a canvas) rather than returning some value.

### nested\_contains

Return whether a list, or any of its sublists, contain some non-list value.

- ▶ should return True if any element is equivalent to value
- should return True if any element is a list ultimately containing value
- Python any and functional if are useful

<expression 1> if <condition> else <expression 2>

If the condition is true, evaluates to the first expression, otherwise evaluates to the second expression.