CSC148, Assignment #2
automated puzzle solving
due March 24th, 10 p.m.
deadline to declare your assignment team: March 18th, 10 p.m.

overview

Puzzle solving is a typically human activity that, in recent decades, is being explored in the context of computers. There are two benefits to this: first, we can off-load some puzzle-solving tasks to computers, and second, we may understand human puzzle-solving better by studying how to implement it on a computer.

This assignment investigates a class of puzzles that have the following features in common:

full information: all information about the puzzle configuration at any given point is visible to the solver; there are no hidden or random aspects

well-defined extensions: a definition of legal extensions from a given puzzle configuration to new configurations is given

well-defined solution: a definition of what it means for the puzzled to be in a solved state is given

These features are common to a very large class of puzzles: crosswords, sudoku, peg solitaire, verbal arithmetic, and so on. This assignment generalizes the required features into an abstract superclass Puzzle, and solving functions are written in terms of this abstract class.

Once this is done, particular concrete puzzles can be modelled as subclasses of Puzzle, and solved using the solving functions. Although there may be faster puzzle-specific solvers for a particular puzzle by knowing specific features of that puzzle, the general solvers are designed to work for all puzzles of this sort.

abstract Puzzle class

The abstract class Puzzle has the following methods, which are not implemented, but meant to be implemented in subclasses:

is_solved: returns True or False, depending on whether the puzzle is in a solved configuration or not

extensions: returns a list of extensions from the current puzzle configuration to new configurations that are a single step ("move") away

fail_fast: returns True or False, depending on whether it is clear that the current puzzle configuration can never be completed, through a sequence of extensions, to a solved state

And that’s it. Notice that there is no __init__ method, since the representation and initialization of puzzles in this class vary widely. Each subclass will need an __init__ method to represent a particular puzzle.
sudoku

This puzzle commonly appears in print media and online. You are presented with an $n \times n$ grid with some symbols, for example digits or letters, filled in. The symbols must be from a set of with $n$ symbols. The goal is to fill in the remaining symbols in such a way that each row, column, or $\sqrt{n} \times \sqrt{n}$ subsquare, has each symbol exactly once. In order for all of that to make sense, $n$ must be a square integer such as 4, 9, 16, 25, ...

You may want to read more about sudoku to get a feel for the puzzle.

We provide you with a mostly-implemented SudokuPuzzle subclass of Puzzle. We, however, did not override the fail_fast method inherited from Puzzle, and you should be able to do better.

Implement fail_fast for sudoku by having it return True for, and hence abandoning, any sudoku configuration where there is at least one empty position that will be impossible to fill because the set of symbols has been completely used up by other positions in the same row, column or subsquare. Experiment to see whether this makes any difference in the performance of solver(s) for sudoku.

peg solitaire

This puzzle has gone by various names: Hi-Q, peg solitaire, solo noble, and patience, and has been around for several hundred years.

You are presented with a grid where most positions are occupied by a peg, marble, or other movable piece. The object is to "jump" a piece over a neighbouring piece and into an empty position, allowing you to remove the piece that was jumped over. A successful game leaves only one piece on the board.

Boards come in various shapes of grid. We will assume that some portion of an $m \times n$ grid is used, that some positions may be unused (no pieces may be placed there), some positions begin with pieces in them, and that a few (often just one) position is left empty to allow jumping. You can see various versions of peg solitaire on the web.

We provide you with the class declaration and _init_ method for subclass GridPegSolitairePuzzle of Puzzle.

You will override the extensions and solved methods for this subclass, which make it possible for the solvers (which you'll also write) to solve it. A legal extension of a GridPegSolitairePuzzle is a new configuration that you can get to in a single jump. The puzzle is solved when a single peg is left.

We do not require you to override the fail_fast method, although you are welcome to see whether you can come up with one that improves performance.

word ladder

This puzzle involves starting with from word, from a set of allowed words, and deriving to word from the same set of allowed words, by changing one letter at a time. Each changed letter must result in a word that is from the same set of words. Here's an example, assuming that the set of words is a rather large set of English words provided to many computer applications. The goal is to get from cost to save

\[
\text{cost} \rightarrow \text{cast} \rightarrow \text{case} \rightarrow \text{cave} \rightarrow \text{save}
\]

We provide you with the class declaration and _init_ method for subclass WordLadderPuzzle of Puzzle.

You will override the extensions and solved methods for this subclass. A legal extension of a WordLadderPuzzle is a new configuration where the from word differs by a single letter from the previous from word. A WordLadderPuzzle is solved when the from word is the same as the to word.
We don’t require you to override the fail fast method, although you are welcome to see whether you can come up with one that improves performance.

mn puzzle

Sometimes called the 15-Puzzle, Boss Puzzle, or Game of 15, this puzzle consists of a $4 \times 4$, $3 \times 3$, or (in general) an $m \times n$, grid with one empty position. A player must swap symbols with the empty position until they get the entire puzzle into the correct order.

We provide the class declaration and _init_ method for subclass MNPuzzle. You will override is solved and extensions methods to allow the solvers to solve this puzzle. The puzzle is solved when the configuration is the same as the supplied target configuration. Legal extensions of a configuration swap the empty space with either the symbol to its right, the symbol to its left, the symbol above it, or the symbol below it.

We don’t require you to override the textbfail_fast method, but you are welcome to see whether you can design one that improves performance.

searching

One approach to solving a puzzle is to systematically search for a solution, starting from the current configuration. To make this daunting task even possible, we have to be sure that we have a systematic way of checking out puzzle configurations, and that we don’t re-visit the same configuration twice.

You will implement two standard systematic searching techniques. We are well aware that plenty of code and pseudo-code for these are "out there" on the web, so you have to be very careful you are giving credit for any ideas you recycle, in order to avoid an academic offense.

depth-first search

As the name suggests, you search deeply before you search broadly.

1. don’t bother with any puzzle configuration if it’s been seen before
2. check whether the current puzzle configuration is solved; if so you’re done; otherwise...
3. for each extension of the current puzzle configuration, make that extension the current puzzle configuration and return to step 1

Notice how this process unwraps. You check a configuration, then one of its extensions, then one of the extension’s extensions, and so on. That means that if a configuration has several extensions, you will be checking every possible chain of extensions from one of them before you check the others.

Notice also that if there are no extensions, step 3 is empty.

You will implement depth_first_solve following this strategy. You are welcome to read material on depth-first search, but be aware of several things:

- the return type for depth_first_solve is a PuzzleNode\(^1\) that must be the first node in a path of PuzzleNodes that lead from the given configuration to a solution
- give credit for ideas from the web that you recycle, so you won’t be guilty of an academic offense.

\(^{1}\)PuzzleNodes are defined in puzzle_tools.py
breadth-first search

As the name suggests, you search broadly before you search deeply.

1. skip any puzzle configuration that has already been seen
2. check whether the current puzzle configuration is solved; if so you’re done, otherwise
3. check whether any extensions of the current puzzle configuration are solved; if so you’re done, otherwise
4. check whether any extensions of extensions of the current puzzle configuration are solved; if so you’re done, otherwise
5. ...

Notice how this approach examines configurations that are “closer” to the starting configuration before it examines those that are “farther.” This may be useful for finding a shortest solution to a puzzle.

You will implement breadth_first_solve following this strategy. You are welcome to read material on breadth-first search, but be warned:

- the return type for breadth_first_solve is a PuzzleNode that is the first node in a path of PuzzleNodes from the current puzzle configuration to a solution
- give credit for ideas from the web that you recycle, so you won’t be guilty of an academic offense

starter code

You’ll find the following files, with associated tasks, in Starter. Leave the class declarations, __init__ methods, and the if __name__ == "__main__" block as you find them: we have verified that neither PyCharm\(^2\) nor PEP8 disapprove of them.

puzzle.py Read and understand the Puzzle class.

sudoku_puzzle.py Read and understand the SudokuPuzzle class, then override the fail_fast method inherited from Puzzle.

grid_peg_solitaire_puzzle.py Read the __init__ method, then override the extensions and is_solved methods inherited from Puzzle.

word_ladder_puzzle.py Read the __init__ method, then override the extensions and is_solved methods inherited from Puzzle.

mn_puzzle.py Read the __init__ method, then override the extensions and is_solved methods inherited from Puzzle.

puzzle_tools.py Read and understand the PuzzleNode class, then implement module-level functions depth_first_solve and breadth_first_solve.

\(^2\)Well, at least, PyCharm Community Edition 5.0.4
declaring your assignment team

You may do this assignment alone or in a team of either 1, 2 or 3 students. Your partner(s) may be from any section of the course on St George campus. You must declare your team (even if you are working solo) using the MarkUs online system.

Navigate to the MarkUs page for the assignment and find “Group Information”. If you are working solo, say so. If you are working with other(s):

First: one of you needs to “invite” the other(s) to be partners, providing MarkUs with their cdf user name(s).

Second: the invited student(s) must accept the invitation.

Important: there must be only one inviter, and other group members accept after being invited, if you want MarkUs to set up your group properly.

To accept an invitation, find “Group Information” on the appropriate Assignment page, find the invitation listed there, and click on “Join”.

submitting your work

Submit the following files on MarkUs by 10 p.m. March 24th:

- sudoku_puzzle.py
- grid_peg_solitaire_puzzle.py
- word_ladder_puzzle.py
- mn_puzzle.py
- puzzle_tools.py

Click on the “Submissions” tab near the top. Click “Add a New File” and either type a file name or use the “Browse” button to choose one. Then click “Submit”. You can submit a new version of a file later (before the deadline, of course); look in the “Replace” column.

Only one team member should submit the assignment. Because you declared your team, all of you will get credit for the work.