

Prep 2 quiz

ⓘ This is a preview of the published version of the quiz

Started: Sep 11 at 1:19pm

Quiz Instructions

Readings

Please read the following part of the [Course Notes](https://www.teach.cs.toronto.edu/~csc165h/winter/resources/csc165_notes.pdf) (https://www.teach.cs.toronto.edu/~csc165h/winter/resources/csc165_notes.pdf) (this includes material we covered in Week 1, but also some new material for Week 2).

- Pages 9–22

General instructions

You can review the general instructions for all prep quizzes at this page. Remember that you can submit multiple times! You might consider printing this quiz out so that you can work on paper first.

Question 1

1 pts

Complete the truth table shown below. **Hint:** you may find it helpful to do this on paper first, and add columns for the intermediate expressions $p \Rightarrow q$ and $q \vee r$.

p	q	r	$(p \Rightarrow q) \Leftrightarrow (q \vee r)$
False	False	False	[Select]
False	False	True	[Select]
False	True	False	[Select]
False	True	True	[Select]
True	False	False	[Select]

True	False	True	[Select]
True	True	False	[Select]
True	True	True	[Select]

Question 2**1 pts**

Recall that two propositional formulas are **equivalent** if they have the same value for all truth assignments to their variables. For example, $p \Rightarrow q$ and $\neg q \Rightarrow \neg p$ are equivalent.

The two formulas $(p \Rightarrow q) \Rightarrow r$ and $p \Rightarrow (q \Rightarrow r)$ are *not* equivalent. Select all of the truth assignments for p , q , and r that make these formulas have *different* values.

 $p = \text{False}, q = \text{False}, r = \text{False}$
 $p = \text{False}, q = \text{False}, r = \text{True}$
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Question 3**1 pts**

Which of the following formulas is logically equivalent to $(p \Rightarrow q) \Rightarrow r$? (You can do this by writing a few truth tables.)

$p \vee \neg q \vee r$

$p \Rightarrow (q \Rightarrow r)$

$r \vee (p \wedge \neg q)$

$(p \vee q) \Rightarrow r$

Question 4**1 pts**

Let U be the set of all New Year's Eve parties, and suppose we define the predicates $P(x)$ and $Q(x)$ over universe U as follows.

- $P(x)$: party x was loud;
- $Q(x)$: party x was boring.

For each English statement below, select its correct translation into predicate logic.

Every party was loud.

Some party was boring.

Some loud party was boring.

Every party was loud or boring (or both loud and boring).

Question 5**1 pts**

Let U be the following set of Christmas presents.

$$U = \{ \text{lump_of_coal}, \text{switch}^{\text{TM}}, \text{pony}, \text{castle} \}$$

Each present has a different price; they are written above in increasing order of price, with lump_of_coal being the cheapest, and castle being the most expensive.

Define the predicate $P(x, y)$ over U as follows:

$P(x, y)$: x is as expensive as y or more expensive than y

For each statement below, select whether it is true or false.

- $\forall x \in U, P(x, \text{pony})$
- $\exists x \in U, P(x, \text{pony})$
- $\forall x \in U, P(\text{castle}, x)$
- $\exists x \in U, P(\text{castle}, x)$
- $\exists x, y \in U, P(x, y)$
- $\forall x, y \in U, P(x, y)$

Saving...

