

CSC165H1: Problem Set 0 Sample Solutions

Due Wednesday September 18 before 4 pm

Note: solutions are incomplete, and meant to be used as guidelines only. We encourage you to ask follow-up questions on the course forum or during office hours. In this problem set, you will **type** a document containing both text and mathematics. Use your favourite word processor, provided it can produce suitable symbols and align equations. If not, you will need to dig through the instructions, or else look at another tool, for example:

Google docs equation editor: See Google Docs equations

L^AT_EX: See L^AT_EXtutorial

1. Create a title for your document that shows our course code (CSC165H1F), the phrase “Problem Set 0”, and the due date.

Solution

CSC165H1 Problem Set 0
due September 18th

2. Create an unordered list (e.g. bullet points) of five foods. Beside each food list a number from 0 to 10 inclusive, where 0 indicates you would **never** eat this food and 10 indicates you would **always** eat this food if given the chance. You must have 5 different numbers.

Solution

- guava: 0
- banana: 10
- artichoke: 5
- cabbage: 7
- rice: 2

3. Let

$$S_1 = \{1130, 1160, 1170, 1180, 1190, 1200, 1210, 1220, 1230, 1240\},$$

and S_2 be the set of all integers that are multiples of 3. List all of the elements in the $S_1 \setminus S_2$ using set notation (i.e., $\{\dots\}$).

Solution

$$S_1 \setminus S_2 = \{1130, 1160, 1180, 1190, 1210, 1220, 1240\}$$

4. Write down the truth table for the propositional formula $(p \vee q) \Rightarrow \neg s$. There should be *eight* rows in your table (plus a header row).

Solution

p	q	s	$(p \vee q) \Rightarrow \neg s$
T	T	T	F
T	T	F	T
T	F	T	F
T	F	F	T
F	T	T	F
F	T	F	T
F	F	T	T
F	F	F	T

5. Show the steps involved in isolating x in the following equation (assume c is positive). Do *not* just show the final result: we're looking for at least two or three steps here, to demonstrate that you can align the equal signs.

$$2^{3x-1} = c^{5x}$$

Remember that *isolating* a variable means rewriting an equation so that the variable appears on one side by itself, and no occurrences of that variable appear on the other.

Hint: Try taking the logarithm base 2 of both sides. You might want to review logarithms if you get stuck here.

Solution

$$\begin{aligned}
 2^{3x-1} &= c^{5x} \\
 \Leftrightarrow 3x - 1 &= 5x \lg(c) \\
 \Leftrightarrow 3x - 5x \lg(c) &= 1 \\
 \Leftrightarrow x(3 - 5 \lg(c)) &= 1 \\
 \Leftrightarrow x &= \frac{1}{3 - 5 \lg(c)} \quad \# \text{ provided } c \neq 2^{3/5}
 \end{aligned}$$