

# Markets and Information (continued)

CSC200 Lecture 45  
Winter 2015

# CSC200: Lecture 45

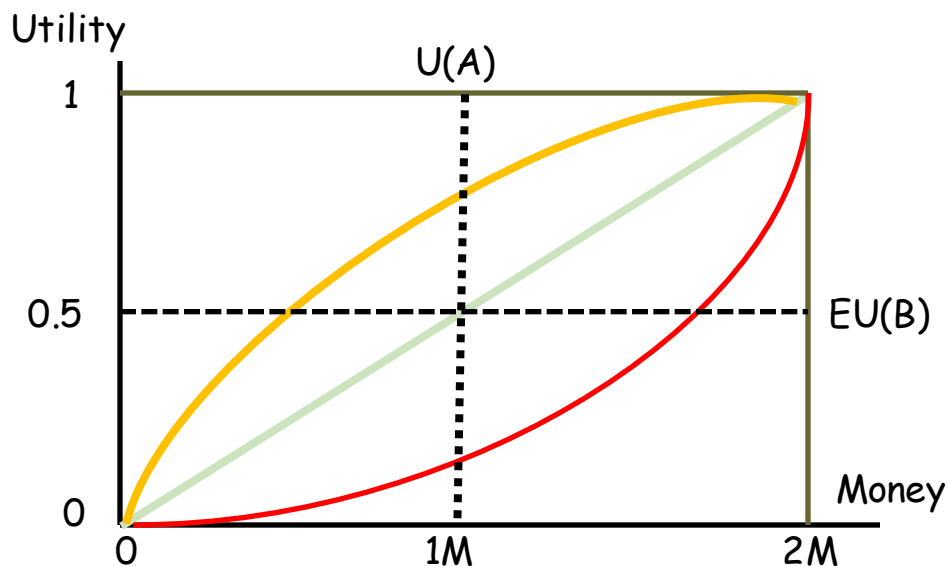
- This week:
  - Finish markets and information (Ch.22 excluding Section 22.10)
- Announcements
  - Check your marks online to make sure they are inserted correctly into the system.
  - Last tutorial this Friday will be devoted to answering questions relating to final exam.
  - I am in my office all day Monday, April 18
  - Scope of final exam: There will be multipart questions on:
    - Game theory (matrix form), stable matchings, matching markets, slot-advertising/VCG/GSP, voting rules, plus some questions on direct benefits, small worlds and Bayes rule
    - And social-affiliation networks: I forgot to mention this previously
- Good way to Review:
  - Look at any assignments and posted solutions

# Markets and Information

- Brief recap of last class (see L37 Slides):
  - Markets for **exogenous** events
    - What is an exogenous event/desirability?
  - Prediction markets
  - Utility for money, risk attitudes, logarithmic utility
  - Optimal betting: betting your beliefs
  - Betting markets, fair odds, state prices (inverse odds)

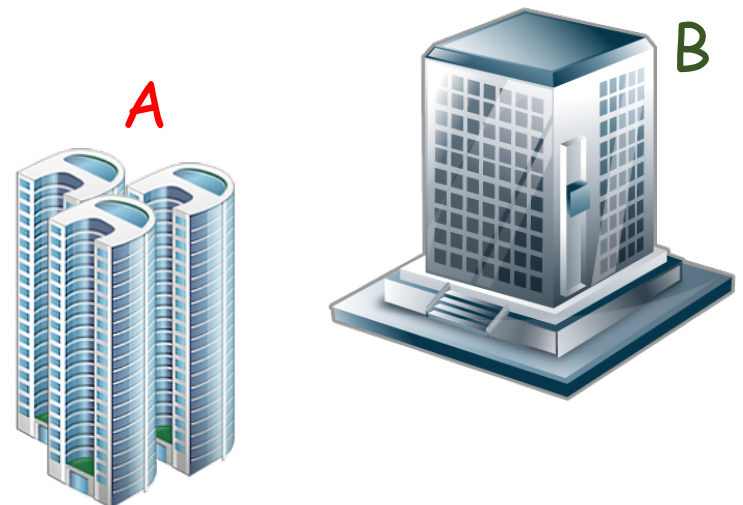
# Review of Risk Attitude (Example)

- What to choose? A: \$1M or B: [(0.5, \$2M), (0.5, 0)]
- Risk-averse person with  $u(w) =$ 
  - A:  $U(1M) = 0.707$     B:  $0.5 * U(2M) + 0.5 * U(0) = 0.5$
- Risk-neutral person with  $u(w) =$ 
  - A:  $U(1M) = 0.5$     B:  $0.5 * U(2M) + 0.5 * U(0) = 0.5$
- Risk-seeking person with  $u(w) =$ 
  - A:  $U(1M) =$     B:  $0.5 * U(2M) + 0.5 * U(0) = 0.5$



# Stock Markets

- If we take a “fundamental” perspective on stock trading, investment in a stock can be viewed in a similar way to prediction markets.
- Investment in a stock: paying for future earnings of some company
  - ignore stock trading, ability to sell for a higher price later, time effects, etc.
  - Simple case: imagine two competing companies **A**, **B**
  - only one will survive, and provide a payout of \$1 per share
  - then we can treat it as a horse race



# Stock Markets



- More generally, many factors impact the payout of a stock
  - economic indicators, R&D outcomes, competitors, new entrants...
  - each outcome corresponds to a **state**, occurs with a certain probability
  - **company value (payout) varies with state**
- Thus it should be that:
  - **probabilities of states (or state prices) determine current value of stock**
  - current value of stock should reflect consensus estimate of state prices

# Two Companies Example (1)

- Suppose just two states  $s_1$  and  $s_2$  (represent relative success of A, B)
- Company A pays out \$2 in  $s_1$ ; \$1 in  $s_2$ ; B pays out \$1 in  $s_1$ ; \$2 in  $s_2$
- **Suppose consensus estimates:**  $Pr(s_1) = 0.75$  and  $Pr(s_2) = 0.25$
- First: state prices should determine value of each stock

## Odds, state price of $s_1$

$$o_1 = 1/0.75 = 4/3$$

$$\rho_1 = 1/o_1 = 3/4$$

## Odds, state price of $s_2$

$$o_2 = 1/0.25 = 4$$

$$\rho_2 = 1/o_2 = 1/4$$

**Value of stock A:**  $v_A = 2\rho_1 + 1\rho_2 = 2(3/4) + 1(1/4) = 7/4$

**Value of stock B:**  $v_B = 1\rho_1 + 2\rho_2 = 1(3/4) + 2(1/4) = 5/4$

# Two Companies Example (2)

- Value of stock (assuming known value of payout at each state) can determine the state prices (odds of each state)
  - In this way, we can view the price of a stock as a prediction of future outcomes.
  - More generally, they place constraints on odds of each state:

Value of stock A:  $v_A = 2\rho_1 + 1\rho_2 = 7/4$

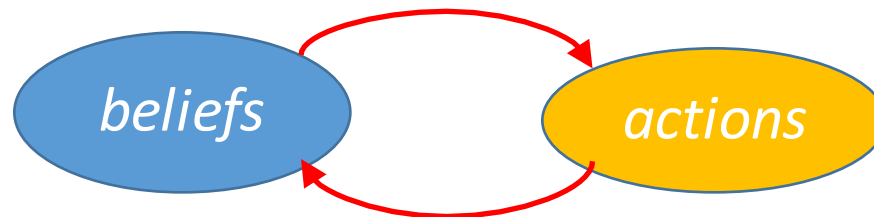
Value of stock B:  $v_B = 1\rho_1 + 2\rho_2 = 5/4$

**Solution to linear system gives state prices:**

$$\rho_1 = \frac{2v_A - v_B}{3} = \frac{3}{4} \quad \rho_2 = \frac{2v_B - v_A}{3} = \frac{1}{4}$$

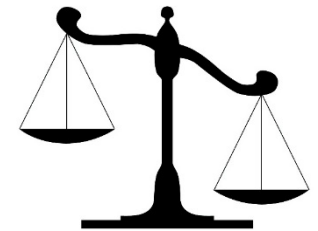
# Markets with Endogenous Events

- We've seen that markets can aggregate opinions, predictions, beliefs of participants with respect to some exogenous event.
- But what if the functioning of the market impacts the event itself? i.e., what if events are endogenous?
  - In this case, people's **expectations or beliefs** about market actions influence the **market actions** themselves, which can in turn influence beliefs, which...
  - This is a form of *self-fulfilling expectations equilibrium*



# Asymmetric Information

- *Asymmetric information*: one side of market has better information about the goods or services offered
- Markets with asymmetric information:
  - Used car market (sellers know more than buyers)
  - e-bay or Amazon (sellers know more than buyers)
  - Health insurance (buyers know more than sellers)
  - Stock Market (either side can have valuable info. on the future value of stock unknown to other)
- It can lead to total market failure.
- Let's start with a simple, but classic example.



# The Market for Lemons



- Consider market for used cars (Akerlof 1970)
  - Two types of cars: *good, bad*
  - Sellers *know* the type of the car they sell
  - Buyers *do not know* the type of the car they buy
  - Good cars worth more than bad
  - Cars are worth more to buyers than sellers
  - Everyone knows fraction of good ( $g$ ) vs. bad ( $1-g$ ) cars for used cars



Car Type	Good	Bad
Value to Seller (\$,000)	10	4
Value to Buyer (\$, 000)	12	6
Relative Fraction	$g$	$1-g$

# Symmetric Information

- Suppose *buyers also knew* if car is good or bad
- Transactions would be clear:
  - good cars would sell for anywhere between \$10-12K
  - bad cars would sell for anywhere between \$4-6K
  - actual prices would be determined by buyer:seller ratio
    - assuming more buyers than sellers, prices push to upper end



Car Type	Good	Bad
Value to Seller (\$,000)	10	4
Value to Buyer (\$,000)	12	6
Relative Fraction	$g$	$1-g$

# Asymmetric Information

- Now return to “sellers know, buyers don’t” scenario
- Let’s assume for now that *all cars (good or bad) are up for sale*
- What is value of purchasing a car to a buyer B?
  - With probability  $g$ , B gets a good car, with probability  $1-g$  a bad car
  - Expected value of car to buyer is  $12g + 6(1-g) = 6 + 6g$
  - Buyers require car prices to be  $p^* \leq 6 + 6g$
- Would any transactions occur?
  - Depends on price  $p^*$  of used cars on the market
  - Good sellers require a price  $p^* \geq 10$  (and bad sellers will charge same!)
  - So feasible price (for selling all cars) exists if  $6 + 6g \geq 10$ ; i.e.,  $g \geq 2/3$
- What would happen if  $g < 2/3$  ?
  - Buyers maximum price is less than 10
  - So no good sellers would sell
  - Only bad cars would hit the market!

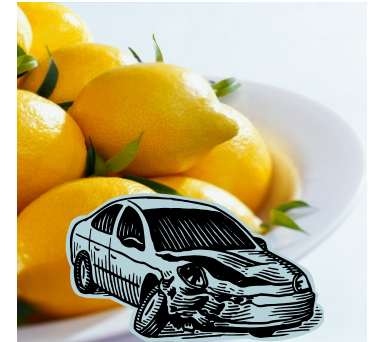
Car Type	Good	Bad
Value to Seller	10	4
Value to Buyer	12	6
Relative Fraction	$g$	$1-g$

# Self-fulfilling expectations equilibria

- B knows  $g$  but not necessarily all  $g$  good cars are on market.
- So B needs to have belief on which portion of good cars are for sale
- Suppose he believes  *$h \leq g$  of cars are good and for sale.*
- B will pay  $p^* \geq 10$  only if  *$h=g$  (i.e., all good cars for sale) and  $2/3 \leq g$ .*
- But if  $h < g$ , Then B's willingness to pay is  $< 10$
- But at that price no good sellers will sell, thus leaving the market.
- We have two *self-fulfilling expectations equilibria* (if  $g \geq 2/3$ )
  - Both  $h=0$  and  $h=g$  are sustainable (no other equilibrium points)
- If  $g < 2/3$  then only equilibrium is  $h=0$
- *Market failure for good cars ( $h=0$ ):*
  - occurs when  $g < 2/3$  but can also occur when  $g \geq 2/3$
  - due solely to the asymmetry in information between buyer and seller

# Multiple Levels of Quality

- Generally, cars come in variable qualities, but impact is same
- Consider a simple three-quality extension
  - good cars, bad cars, and “lemons” (worthless), say, in equal proportions
  - again, sellers know quality, buyers do not
- Let’s see what happens...



Car Type	<i>Good</i>	<i>Bad</i>	<i>Lemon</i>
Value to Seller (\$,000)	10	4	0
Value to Buyer (\$, 000)	12	6	0
Relative Fraction	1/3	1/3	1/3

# Lemons can “Infect the Market”

- If buyers believes all cars are on the market:
  - expected value to buyers is  $(12+6+0)/3 = 6$ : max. price buyers will pay
  - less than price 10 required by good sellers, so...
  - *no good cars will be on the market*: not an equilibrium
  - note: this price would support bad sellers; except...
- If buyers believe only bad cars and lemons are on the market:
  - expected value to buyers is  $(6+0)/2 = 3$ : max. price buyers will pay
  - less than price 4 required by bad sellers, so...
  - *no bad cars will be on the market*: not an equilibrium
- Only equilibrium is for lemons to be sold: *complete market failure*



Car Type	Good	Bad	Lemon
Value to Seller	10	4	0
Value to Buyer	12	6	0
Relative Fraction	1/3	1/3	1/3

# Signaling Quality

- Information asymmetry can powerfully affect the operation of a market.
- How to mitigate the effect of information asymmetry?
  - signaling quality might help.
- If seller can signal some reliable indicator of quality, it can improve the prospects of good cars
  - E.g., some dealers guarantee that a used car is a “certified used car”: checked for certain problems/defects and repaired if needed.
  - Some dealers provide short-term warranties in used cars



# Labor markets

- Labor markets
  - Workers offering services of various qualities to employers
  - Workers have better idea of their skills than employers
  - Interviews help, but only partially (just like car inspection)
  - Skill-full workers can always be self-employed.
  - Information asymmetry can drive good workers out of market.
- Signaling Quality:
  - E.g., investment in education as signaling
  - Your CS degree: indication of productivity/intelligence even if you work in another area

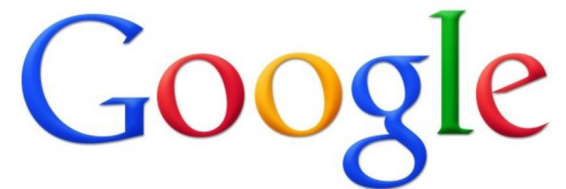
# Health Insurance Market

- Insurance markets: very asymmetric information
  - Buyers of insurance: more info about their health than Insurance comp.
  - Expected payout per policy is avg. of payout to people in poor health and people in good health
- Thus people in good health *pay more than their expected return*
  - If pool of insured has many poor-health folks, may drive out some healthy people
  - So policy costs to go up, which drives out more healthy people, ...
  - Soon: only people with very poor health participate
  - Insurance company charges full expected cost
  - Phenomenon known as *adverse selection*.
- How can this be mitigated in practice?



# Other Issues

- Relation to crowdsourcing: think about it...
- Relation to online selling (e.g., E-Bay)
  - Reputation mechanisms
  - False-names/identities may circumvent
- Relate to ad auctions
  - Why is it in Google's interests to prevent spammers (irrelevant ad posters) from posting ads that induce a lot of clicks (hence revenue for Google)?



# Wrapping up: The Big Picture

- What have we covered and how does it all fit together?
- **Types of Networks**
  - Social Networks: people interacting in various relationships
  - Affiliation Networks: people interacting with institutions
  - Physical Networks: traffic networks, internet, etc.
  - Economic Networks: trading networks, marriage markets, kidney exchange, ...
  - ...
- **How Networks Shape Information Flow and Behavior**
  - closure properties: how relationships spread
  - information diffusion: how information spreads
  - technology diffusion: how behaviors spread
  - epidemics: how diseases spread
  - ...

# The Big Picture Continued

- **Explaining Interactions at the Micro-level**
  - Game theory: how people choose behaviors: incentives, equilibria
  - Probabilistic reasoning: how evidence (personal as well as behavior of others) shapes one's beliefs
- **How Micro-interactions Manifest at Macro-level**
  - information cascades
  - positive externalities/network effects (tipping points)
  - technology diffusion (*\*one of only a few with network playing a role*)
  - power laws
  - small worlds/search (*\*one of only a few with network playing a role*)
  - epidemics (*\*one of only a few with network playing a role*)
  - prediction markets and market failures
  - voting (both info and preference aggregation)

# Discuss: There are Lots (!) of Gaps

- The influence of networks on micro-formation of beliefs and preferences, macro-level behavior is still poorly understood
  - how do social networks influence people preferences, voting behavior, economic interactions, beliefs/biases?
  - lots of current research going on: but in its infancy...
- The influence of micro-level preferences, beliefs, existing relationships on the formation of networks also poorly understood
  - how do existing relationships, beliefs, preferences all come together to influence to formation and dissolution of network ties?
  - lots of partial models, abstract mathematical models, but...
- **Beyond** “understanding”: How do we design, shape, exploit networks to help people become better informed, form desired relationships, make better decisions, of help shape their behavior?

# How can we make the course better?

- Topics

- What would you like to see more/less of?
- What was missing that should have been here?
- Style, emphasis:
  - Mathematical modeling/analysis
  - Algorithms, programming, computation
  - Interdisciplinary: not enough? Too much?
  - Rigor and formality...
- Background Needed
- Materials, text, slides, assignments, tests...
- CS vs. non-CS students: how do we attract more of each?
- Next year: half course focused more on economic models, game theory



