

- A2 - 8 days (approx), extra office hours next week
- E6 up this aft (last exercise...).

CSC148 fall 2013

binary search tree

week 8

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Outline

performance

binary search tree

big-oh

performance...

We want to measure **algorithm** performance, independent of **hardware** programming language, random events

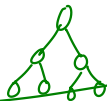
→ elements in a list, e.g.

Focus on the **size of the input**, call it n . How does this affect the resources (e.g. processor time) required for the output? If the relationship is linear, our algorithm's complexity is $O(n)$ — roughly proportional to the input size n .

list searching

$$O(\lg n)$$

$$n \leq 2^k$$
$$\lg n \leq k$$



$$\frac{n}{2^k} \leq 1$$

list size n

$$\frac{n}{2^k} \leq 1$$

You've already seen algorithms for seeing whether an element is contained in a list:

[97, 36, 48, 73, 156, 947, 56, 236]

What is the performance of these algorithms in terms of list size? What about the analogous algorithm for a tree?

linear search. $O(n)$

if list is already sorted, try binary search.

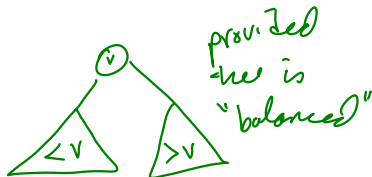
$O(\lg n) \rightarrow$
binary search.



a more efficient binary tree

We need to impose a sorting condition on binary trees. A **binary search tree** is:

- ▶ a binary tree ✓



- ▶ left subtree of every node contains only values smaller than those of that node
- ▶ right subtree of every node contains only values greater than those of that node

efficiency?

Binary search of a list allowed us to ignore (roughly) half the list. Searching a binary search tree allows us to ignore the left or right subtree.

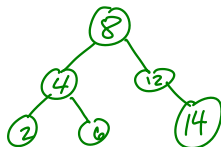
→ AVL trees, red-black trees.

If we're searching the tree rooted at node n for value v , then one of three situations are possible:

- ▶ node n has value v
- ▶ v is less than node n 's value, so we should search to the left
- ▶ v is more than node n 's value, so we should search to the right

ignore entire subtrees.

insert



Inserting is closely related to finding a node:



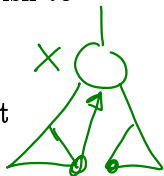
- ▶ if we find a node in our tree, no need to insert it!
- ▶ otherwise, we find the spot it should be, and insert it there.

deleting



deleting is a bit trickier, because there are several scenarios to consider, even after we've figured out which node we wish to delete:

- ▶ if the node we wish to delete is a leaf, just delete it
- ▶ if the node we wish to delete has exactly one child, replace it with the other
- ▶ if the node we wish to delete has two children, replace it with the largest child in its left subtree...



You should draw some diagrams until you understand these scenarios

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