

CSC104 fall 2013  
Computational thinking  
week 5

Danny Heap  
heap@cs.toronto.edu  
BA4270 (behind elevators)

<http://www.cdf.toronto.edu/~heap/104/F12/>  
416-978-5899

Text: **Picturing Programs**

# Outline

Representing information

Notes

# Some convergence

digital, binary, small, fast, cheap...

Computers have converged on two general design ideas:

**digital:** Using discrete, sharply-changing, rather than analog, smoothly-changing states

**binary:** Two states is the smallest, most easily designed



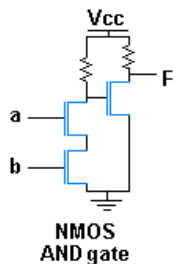
memory should be reliable  
fast, and cheap  
magnetic (left), transistor (right)



# Boolean logic

## simple operators

Two values, **true** and **false** can be combined:

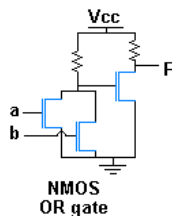


a	b	(and a b)
true	true	true
true	false	false
false	true	false
false	false	false

# Boolean logic

more simple operators

Two values, **true** and **false** can be combined:

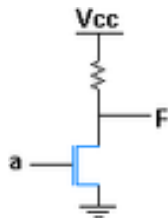


a	b	(or a b)
true	true	true
true	false	true
false	true	true
false	false	false

# Boolean logic

one more simple operator

Single value, **true** or **false** can be transformed:



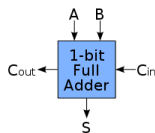
**NMOS  
NOT gate**

a	(not a)
true	false
false	true

# Boolean arithmetic

## bitwise operator

Two values, 0 or 1, can be combined:



A	B	C <sub>in</sub>	C <sub>out</sub>	S
0	0	0	0	0
1	0	0	0	1
0	1	0	0	1
1	1	0	1	0
0	0	1	0	1
1	0	1	1	0
0	1	1	1	0
1	1	1	1	1

binary, decimal...

5897 — multiply each digit by the appropriate power of 10

$$\underbrace{5 \times 10^3}_{5000} + \underbrace{8 \times 10^2}_{800} + \underbrace{9 \times 10^1}_{90} + \underbrace{7 \times 10^0}_{7}$$

- ▶ What happens when you add zeros on the right — 58970  
589700?
- ▶ What happens when you drop digits from the right — 589,  
58?
- ▶ Can you guess at a general rule?



binary, decimal...

1011 multiply each digit by the appropriate power of 2

$$\underbrace{1 \times 2^3}_8 + \underbrace{0 \times 2^2}_0 + \underbrace{1 \times 2^1}_2 + \underbrace{1 \times 2^0}_1$$

- ▶ What happens when you add zeros on the right — 10110, 101100?
- ▶ What happens when you drop digits from the right — 101, 10?
- ▶ Can you guess at a general rule?

## number to binary

How do you write 37 in binary?

- ▶ Suppose you knew it had six **binary digits (bits)**, ??????. Does the fact that 37 is odd help you know whether the bit on the right is a 0 or 1?
  
- ▶ Suppose you know what the digit on the right is. What connection is there between the remaining bits, ?????, and  $37/2$  (rounded down)?

# Notes

