

T1 - handed back after class, grades already posted online  
average 78%<sup>90</sup>

😊

↳ "hard questions"

Q1, Q6

≈ 60%

## CSC104 fall 2012

Why and how of computing  
week 6

Rubric  
on part II  
tomorrow.

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Text: **Picturing Programs**



# Outline

algorithms questions

Notes

# could algorithms run the world?

Spectacular algorithm success leads to questions:

- ▶ Is there, potentially, an algorithm to solve every problem?

*No*

- ▶ If there are two or more algorithms solving the same problem, how do you choose? *compare efficiency*

- ▶ How do you discover new algorithms?

*Heuristics - tips no guarantee*

- ▶ How do you maintain and improve massive, possibly buggy, algorithms?



# problems without an algorithm



before electronic, programmable  
computers

Alonzo Church and Alan Turing  
showed there were many  
unsolvable algorithms



*— also showed class of solvable algorithms*

Classic example: **Halting Problem**

## another example

If there an algorithm for each problem, how about one to decide whether declarative English sentences are true? How about:

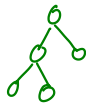
This statement is false.

What should the algorithm that verifies (or not) sentences do?

## algorithms that take too long

$$\begin{aligned} \text{fib}(0) &= 0 \\ \text{fib}(1) &= 1 \end{aligned}$$

$$\begin{aligned} \text{fib}(2) &= \text{fib}(0) + \text{fib}(1) = 1 \\ \text{fib}(3) &= \text{fib}(1) + \text{fib}(2) \\ &= \text{fib}(0) + \text{fib}(1) + \text{fib}(1) \end{aligned}$$



An algorithm may exist, but take too long to be feasible:

```
(define (fib n)
  (if (< n 2)
      n
      (+ (fib (- n 1)) (fib (- n 2)))))
```

$$\begin{aligned} \text{fib}(4) &= \text{fib}(2) + \text{fib}(3) \\ &= \text{fib}(0) + \text{fib}(1) + \text{fib}(1) + \text{fib}(2) \\ &= \text{fib}(0) + \text{fib}(1) + \text{fib}(1) + \text{fib}(0) + \text{fib}(1) \end{aligned}$$

*rewrite several efficient ways.*

Of interest from rabbit-breeding to biology to computer science (see [Vi Hart](#)), calculating Fibonacci sequence **this way** gets slow for numbers over 40.



# how to solve it

it being a new problem

Clearly there's no fool-proof method, but there's some **techniques that often make progress**. It helps to write down the whole process:

- ▶ Understand the problem

draw pictures use symbols

- ▶ Devise (one or more) plan(s)

breadth-first search versus depth-first search.

- ▶ Try the plan

- ▶ Look back

what's required  
what's given  
; solver-name: input → output





# paper folding?

try it out

centre the patterns — so that first fold is visible  
↑↓  
- given natural number  
- need pattern "up" "down"  
- Ds and Us

- ▶ Understand the problem (what's given, what's required)?
- ▶ Devise a plan chop # folds # crease pattern  
- small examples → looking for a pattern.  
- working backward.
- ▶ Try at least one plan (be ready to abandon it too)

▶ Look back

# Notes

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