Question 1. [5 marks]

Read over the declaration of class BTNode as well as the header and docstring for function has_ordered_cluster. Then complete the implementation of has_ordered_cluster.

class BTNode:
    """A node in a binary tree."""

def __init__(self: 'BTNode', item: object, 
    left: 'BTNode' =None, right: 'BTNode' =None) -> None:
    """Initialize this node.
    """
    self.item, self.left, self.right = item, left, right

def has_ordered_cluster(T: BTNode) -> bool:
    """Return true if tree rooted at T has a node with
    node.left.item < node.item < node.right.item
    """
    if T is None:
        return False
    else:
        return ((T.left and T.right and T.left.item < T.item < T.right.item) or
                has_ordered_cluster(T.left) or
                has_ordered_cluster(T.right))

Marking notes: 1 mark for None base case, 2 marks for checking whether the root T is involved in a "cluster", 2 marks for recursively checking T.left and T.right.

Question 2. [5 marks]

Read over the declarations of classes BTNode and LLNode, as well as the header and docstring for function root_to_leaves. Then implement the function root_to_leaves.

class BTNode:
    """A node in a binary tree."""

def __init__(self: 'BTNode', item: object,
class LLNode:
    """A node in a linked list.""

    def __init__(self: 'LLNode', item: object, link: 'LLNode' = None) -> None:
        """Initialize this node.
        ""
        self.item, self.link = item, link

    def __repr__(self: 'LLNode') -> str:
        """Return a string that represents self in constructor (initializer) form.
        >>> b = LLNode(1, LLNode(2, LLNode(3)))
        >>> repr(b)
        'LLNode(1, LLNode(2, LLNode(3)))'
        ""
        return ('LLNode({}, {})'.format(repr(self.item), repr(self.link))
                if self.link else 'LLNode({})'.format(repr(self.item)))

    def __eq__(self: 'LLNode', other: 'LLNode') -> bool:
        """Return whether LLNode self is equivalent to LLNode other"
        return (isinstance(other, LLNode) and
                self.item == other.item and self.link == other.link)

def root_to_leaves(T: BTNode) -> list:
    """Return list of paths from T to each of its leaves, or [] if T is None. Each path is a linked list formed from LLNodes. You may decide whether or not to return a single-node linked list when T has no children.
    >>> T = BTNode(1, BTNode(2, None, BTNode(3)), BTNode(4, BTNode(5), BTNode(6)))
    >>> L1 = root_to_leaves(T)
    >>> L2 = [LLNode(1, LLNode(2, LLNode(3))), LLNode(1, LLNode(4, LLNode(5))), 
                LLNode(1, LLNode(4, LLNode(6)))]
    >>> len(L1) == len(L2) and all([p in L2 for p in L1])
    True
    ""
    if T is None:
return []
elif T.left is None and T.right is None:
    return [(LLNode(T.item, None))]
else:
    leftchpaths = root_to_leaves(T.left)
    rightchpaths = root_to_leaves(T.right)
    leftpaths = [LLNode(T.item, P) for P in leftchpaths]
    rightpaths = [LLNode(T.item, P) for P in rightchpaths]
    return leftpaths + rightpaths

Question 3. [5 MARKS]

Read over the class declaration for BTNode and the header and docstring for function ordered_and_bounded. Then implement ordered_and_bounded.

class BTNode:
    """A node in a binary tree."""

    def __init__(self: 'BTNode', item: object, 
                 left: 'BTNode' = None, right: 'BTNode' = None) -> None:
        """Initialize this node."
        self.item, self.left, self.right = item, left, right

def ordered_and_bounded(T: BTNode, lower: int, upper: int) -> list:
    """Return a list of items, in ascending order, from nodes of T, 
    with all items no less than lower and no greater than upper. 
    Return [] if T is None. You are *not* allowed to sort any list, and 
    you should visit as few nodes as possible.
    preconditions: -- node items in T are comparable, 
    -- T is a binary search tree in ascending order, 
    that is, all items in every left sub-tree are less 
    than the sub-tree’s root and all items in every right 
    sub-tree are more than the sub-tree’s root

    >>> T = BTNode(4, BTNode(2, BTNode(1), BTNode(3)), BTNode(6, 
    BTNode(5), BTNode(7)))
    >>> ordered_and_bounded(T, 2, 5)
    [2, 3, 4, 5]
    """

    if T is None:
        return []
def hybrid_search(x:int,L:list) -> bool:
    """precondition: L is sorted"
    >>> L = [1,5,9, 9, 9, 12, 12, 15, 19,20,40,41,42,43,50,100,500]
    >>> hybrid_search(21,L)
    False
    >>> hybrid_search(100,L)
    True
    """
    def helper(i,j) -> bool:
        # precondition: 0 <= i <= j < len(L)
        if (j-i) < len(L)/10:
            return any([y == x for y in L[i:j+1]])
        if x < L[(i+j)//2]:
            return helper(i, (i+j)//2-1)
        elif x > L[(i+j)//2]:
            return helper((i+j)//2+1, j)
        else:
            return True
    return helper(0,len(L)-1)
def hybrid_search2(x:int,L:list) -> bool:
    """precondition: L is sorted
    >>> L = [1,5,9, 9, 9, 12, 12, 15, 19,20,40,41,42,43,50,100,500]
    >>> hybrid_search(21,L)
    False
    >>> hybrid_search(100,L)
    True
    """
    def helper(i,j) -> bool:
        # precondition: 0 <= i <= j < len(L)
        if (j-i) < 10:
            return any([y == x for y in L[i:j+1]])
        if x < L[(i+j)//2]:
            return helper(i, (i+j)//2-1)
        elif x > L[(i+j)//2]:
            return helper((i+j)//2+1, j)
        else:
            return True
    return helper(0,len(L)-1)
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# 3: _____/ 5
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