CSC104 fall 2012
Why and how of computing
week 7

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Text: Picturing Programs
Outline

convert to binary

More numbers

characters, images, sound

Really crude encryption

Notes
How do you write $37$ in binary?

- Suppose you knew it had six binary digits (bits), ?????. Does the fact that 37 is odd help you know whether the bit on the right is a 0 or 1?

- Suppose you know what the digit on the right is. What connection is there between the remaining bits, ?????, and $37/2$ (rounded down)?
Once we can add non-negative integers, we can multiply them with a small number of additional operations. Consider the binary multiplication table:

<table>
<thead>
<tr>
<th>×</th>
<th>0</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

I use this to multiply the binary representations of 15 and 19. Other arithmetic functions are implemented as particular circuits.
Negative numbers, fractions
reassign some bits

Sometimes the left-most bit is used to represent + (as 0) or — (as 1). Another (efficient) scheme is called two’s complement.

In base 10, by shifting a number right (past the decimal point) we multiply it by 1/10. In binary, we shift right past the binary point, and reduce by 1/2.

\[
1.01 = \frac{5}{4} = 1\frac{1}{4} \quad 101 = 5 \quad 10.1 = 5\frac{1}{2} = 2\frac{1}{2}
\]

A common scheme, called IEEE floating point, uses 64 bits (binary digits): one for the sign, 11 for the magnitude (from \(2^{-1022}\) to \(2^{1023}\)) and the remainder for an non-negative integer.
Enough numbers!

what about text?

7 bits is enough to represent 128 values: upper- and lower-case latin characters, 10 numerals, some punctuation, and special control characters.

More than 110,000 characters can be specified with unicode (using more than 7 bits each).
What about images

how do those pixels glow so?

Computers represent images as rectangular arrays of glowing pixels. There are various schemes to determine what colour each pixels glows, one is **rgba**, which is what we use in picturing-programs

\[
\begin{array}{c}
256 \\
\downarrow \\
\downarrow \\
\downarrow \\
\end{array}
\begin{array}{c}
256 \\
\downarrow \\
\downarrow \\
\downarrow \\
\end{array}
\begin{array}{c}
256 \\
\downarrow \\
\downarrow \\
\downarrow \\
\end{array}
\begin{array}{c}
256 \\
\downarrow \\
\downarrow \\
\downarrow \\
\end{array}
\begin{array}{c}
\alpha \\
\downarrow \\
\downarrow \\
\downarrow \\
\end{array}
\]

Each colour is a value between 0 and 255 (inclusive). This allows \(2^{32}\), over 4 billion colours. The “alpha” band represents opacity from clear (0) to opaque (255).
All the complexity of a room full of instruments can be simulated using a stream of numbers. After all, you can model sound as the displacement of your eardrum one way or the other. That’s what the WAV sound format, a variety of LPCM (Linear Pulse Code Modulation) does.
a blast from the past
really bad text encryption

Encrypt “STRING” → “FGEVAT”
rot13 as an algorithm

- What is given, what’s required?

- Redo the last step for a single character

- What is a really simple rule (or set of rules) for (rot13 c), where c is some character?

- It might help to know that characters A through Z have ascii encodings 65 through 90.
What about characters that aren’t in #\A through #\Z?

What about lower-case characters?

How do we get from characters to strings of characters?
reversing strings

Give step-by-step instructions to reverse “string”

- given/required?

- check-expect some small examples?

- try to write down a recipe
How do you recognize a palindrome, such as “rotor” or “ACTAGATCA”?

- given/required?
- check-expect a small example or two
- try to state the recipe