This test consists of 4 questions on 10 pages (including this one). When you receive the signal to start, please make sure that your copy of the test is complete.

If you use any space for rough work or need to scratch out an answer, circle the part that you want us to mark.

You may write in pencil, however, work written in pencil will not be considered for remarking.

Good Luck!
Question 1. [12 marks]

Consider this schema for Twitter, a social media platform where users post messages called “tweets”.

**Relations**

User(userID, name, email)
A Twitter user.

Tweet(tweetID, userID, content, day)
The user with userID made a tweet containing content on day.

Follows(a, b)
User a follows user b on Twitter, which means that a has subscribed to b’s tweets.

Likes(who, what, d)
User who liked tweet what on day d.

**Integrity Constraints**

Tweet[userID] ⊆ User[userID]
Follows[a] ⊆ User[userID]
Follows[b] ⊆ User[userID]
Likes[who] ⊆ User[userID]
Likes[what] ⊆ Tweet[tweetID]

**Part (a) [2 marks]**

Does the schema enforce this constraint: A user cannot like the same tweet twice? Circle one:

Yes      No.

If yes, explain; if not write a new constraint to enforce it:

**Part (b) [2 marks]**

Does the schema enforce this constraint: You can’t follow yourself? Circle one:

Yes      No.

If yes, explain; if not write a new constraint to enforce it:

**Part (c) [1 mark]**

Suppose relation Likes has 300 tuples. How many tuples could Users have? Circle all that apply:

0      1      256     300     912
Part (d)  [2 marks]

Suppose relation User has \( m \) tuples and relation Tweet has \( n \) tuples. What is the maximum number of tuples that relation Likes can have?

Explain how the schema imposes this limit:
Part (e)  [3 marks]

Suppose we add the following constraint: Likes[who] ⊆ Follows[b]. Make the smallest possible non-empty instance of relations Likes and Follows that violates this constraint:

Express this constraint in English:

What kind of constraint is it? Circle all that apply:

referential integrity constraint  foreign-key constraint  integrity constraint

Part (f)  [2 marks]

Which of the following queries can be expressed using the same form of relational algebra that we used in class and on Assignment 1, that is: the operators Π, σ, ▷◁condition, ×, ∪, −, ρ and assignment? Circle all that apply.

1. Find everyone who follows 6 or more people who have never liked a tweet.
2. Let’s say user X is “upstream” of Y if either X follows Y, or X follows someone else who is upstream of Y. Find every user who is upstream of the person with userID ‘Oprah’.
3. Find the second last tweet from the person with userID ‘Oprah’.
4. Find the user who follows the most people.
5. Find the user who made the first tweet.
Question 2. [8 marks]

Here is the schema from Assignment 1. A few attributes and relations have been omitted for simplicity.

**Relations**

**Product**<br>\( (\text{DIN}, \text{manufacturer}, \text{name}, \text{form}, \text{schedule}) \)<br>A tuple in this relation represents a drug product.

**Price**<br>\( (\text{DIN}, \text{price}) \)<br>The price of a drug product.

**Prescription**<br>\( (\text{RxID}, \text{date}, \text{patient}, \text{drug}, \text{doctor}) \)<br>A prescription for \text{drug} was written on \text{date} for \text{patient} by \text{doctor}. Attribute \text{patient} is the patient’s OHIP number.

**Filled**<br>\( (\text{RxID}, \text{date}, \text{pharmacist}) \)<br>Prescription \text{RxID} was filled by \text{pharmacist} on \text{date}.
Attribute \text{pharmacist} is the pharmacist’s OCP number.

**Integrity constraints**

\[ \text{Price}[\text{DIN}] \subseteq \text{Product}[\text{DIN}] \]

\[ \text{Prescription}[\text{drug}] \subseteq \text{Product}[\text{DIN}] \]

\[ \text{Filled}[\text{RxID}] \subseteq \text{Prescription}[\text{RxID}] \]

\[ \Pi_{\text{schedule} \subseteq \text{Product}} \subseteq \{ \text{“prescription”}, \text{“narcotic”}, \text{“OTC”} \} \]

Write a query in relational algebra to report the OHIP number of every patient who has had a prescription that (a) was for the most expensive drug product (or a product tied for most expensive) and (b) they never filled.

Use only the basic operators \( \Pi, \sigma, \bowtie, \times, \cap, \cup, -, \rho \), and assignment.
Continue your answer here if more space is needed.
Question 3.  [6 marks]

Suppose we have implemented the Twitter schema from Question 1 in SQL, and the tables currently contain the following:

Profile:
| userid | name          | email               |
|--------+--------------+---------------------|
| adele  | Adele Adkins |                     |
| drizzy | Drake        |                     |
| potus  | Barack Obama | potus@gov.us        |
| rjm    | Renee Miller | rjm@cs              |

Follows:
<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>potus</td>
<td>drizzy</td>
</tr>
<tr>
<td>drizzy</td>
<td>rjm</td>
</tr>
</tbody>
</table>

Tweet:
<table>
<thead>
<tr>
<th>tweetid</th>
<th>userid</th>
<th>content</th>
<th>day</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>adele</td>
<td>Hello</td>
<td>2016-10-16</td>
</tr>
<tr>
<td>61</td>
<td>adele</td>
<td>It's me</td>
<td>2016-10-16</td>
</tr>
<tr>
<td>33</td>
<td>potus</td>
<td>6 weeks</td>
<td>2016-10-11</td>
</tr>
<tr>
<td>28</td>
<td>rjm</td>
<td>in the 6</td>
<td>2016-10-10</td>
</tr>
</tbody>
</table>

Likes:
<table>
<thead>
<tr>
<th>who</th>
<th>what</th>
<th>d</th>
</tr>
</thead>
<tbody>
<tr>
<td>drizzy</td>
<td>61</td>
<td>2016-10-18</td>
</tr>
<tr>
<td>rjm</td>
<td>33</td>
<td>2016-10-17</td>
</tr>
<tr>
<td>drizzy</td>
<td>15</td>
<td>2016-10-16</td>
</tr>
<tr>
<td>potus</td>
<td>15</td>
<td>2016-10-16</td>
</tr>
</tbody>
</table>

Show the output of each of the queries below. If a query will not run successfully, write “Illegal”.

```
SELECT who 
FROM Likes JOIN Tweet ON what = tweetID
WHERE userID = 'adele';

SELECT userID, count(tweetID), count(day)
FROM Tweet
GROUP BY userID;

SELECT count(*) AS num1, count(email) AS num2
FROM Profile;

SELECT name, content
FROM Profile NATURAL RIGHT JOIN Tweet;
```

```
SELECT useriD, count(tweetID), count(day)
FROM Tweet
GROUP BY useriD;
```
SELECT tweetID, count(who) 
FROM Tweet, Likes 
WHERE tweetID = what;

(SELECT a AS userID
FROM Follows
WHERE b = 'drizzy')
UNION ALL
(SELECT userID
FROM Tweet
WHERE content like '%6%');
Question 4. [4 marks]

Write a query to find the userID of everyone who has made more than one Tweet. Ensure that it would work on any instance of the database, not simply the one above.
# 1: _____/12
# 2: _____/ 8
# 3: _____/ 6
# 4: _____/ 4

TOTAL: _____/30